# Introduction

For this assignment, using a 3D MRI brain image data (*sub-11\_T1w.nii.gz*), we want to:

* Implement the Geometry Preserving Anisotropic Diffusion Filter (**GPAD**)
* Examine effects of smoothing on edges by enlarging over a small Region of Interest (ROI) using slices 102 and 119.
* Quantify the GPAD filter performances by calculating per voxel squared error difference between smoothed data and original non-noisy data.
* Analyze mean square error (MSE) for three noise levels (10,20 and 30) and five filters: Gaussian, Median, Bilateral, Scalar diffusion and GPAD filter.

# Main Work

1. We upload the NIFTI image **sub-11\_T1w.nii.gz** from the folder data. Make sure that the folder exists with the file. If not, please modify the line: *vol = niftiread('data/sub-11\_T1w.nii.gz')* to point to the location with the file.
2. The image is flipped to facilitate image manipulation.
3. Before starting any filtering, we run a grid search, looking for the optimal parameters of the filter with the lowest root mean squared error. Unless needed; please do not uncomment this part as it is resource intensive and takes a while.

We found that best parameters to obtain the lowest MSE as follows:

|  |  |  |  |
| --- | --- | --- | --- |
| Parameter | Description | Range | Optimal Parameter |
| T | Number of iterations | [5, 10, 15] | 10 |
| dt | Time increment | [0.1, 0.2, 0.3] | 0.2 |
| σg | Width of Gaussian for smoothing the gradient | [0.5, 1, 1.5] | 1 |
| σs | Width of Gaussian for smoothing the structure matrix | [1, 2, 3] | 2 |
| a1 | Diffusion parameter (along contour) | - | 0.5 |
| a2 | Diffusion parameter (perpendicular to contour) | - | 0.9 |

1. Different levels of noise are generated (**applyNoise**) with different scale levels: 10,20 and 30. Noisy slices, 102 and 119 are plotted with their noise levels. (Fig. 1)

A close-up of a brain

Description automatically generated

**Fig.1:** slices 102 and 119 with different noise levels (10,20 and 30).

1. The brain MRI image is smoothed using the GPAD filter.

* TschumperleDeriche Filter is implemented in the function **GeometryPreservingAnisotropicDiffFilter,** which takes as input parameters:
  + I: a 2D image
  + T: number of iterations
  + dt: time increment
  + σg: width of Gaussian for smoothing the gradient
  + σs: width of Gaussian for smoothing the structure matrix G
  + a1 anda2: diffusion parameters for direction of min//mx variations

The algorithm returns the modified image I.

**Geometry Preserving Anisotropic Diffusion Filter** **Algorithm**

A paper with text and images

Description automatically generated with medium confidence

Notice that A and H are two symmetric matrices, thus we can take advantage of MATLAB vectorization to compute the trace using elementwise multiplication (see **computeBAndBetaMax** function):

B(k, :, :) = A11 .\* H11 + 2 \* A12 .\* H12 + A22 .\* H22;

1. We examine effects of smoothing on edges

* We examine the effects of smoothing on edges by extracting a small Region of Interest (ROI) using slices 102 and 119. We call the function **getROI** to retrieve the ROIs for slices 102 and 119 from the noise images (level 10, 20 and 30) and from the smoothed image generated by the GPAD filter.

We then, display the ROIS at each noise level and their smoothed equivalent from the image processed using the GPAD filter for slices 102 and 119 (Fig. 2,3 and 4).

A close-up of a brain

Description automatically generated

**Fig. 2:** At Noise Level 10: The first row displays the noisy ROI of slice 102 on the left, followed by its filtered versions using the GPAD filter on the right. The second row shows the noisy ROI of slice 119 on the left, along with its filtered versions using the same filter.

The subsequent plots illustrate similar information for ROIs at noise levels 20 and 30.

A close-up of a brain

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**Fig. 3.:** noisy ROIS at level 20, and its smoothed ROIS using

GPAD filter.

A close-up of a brain

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**Fig. 4.:** noisy ROIS at level 30, and its smoothed ROIS using

GPAD filter.

* Both slices (102 and 119) display similar patterns with each filter; however, the variation in structure between the two slices highlights the filters' differential impacts on distinct anatomical features.
* Slice 119 ROI have more complex structures that test the filters' ability to preserve edges without introducing artifacts, especially at higher noise levels.

Examining these different images of slices 102 and 119, we observe:

* That the filter successfully maintains clear and well-defined edges, even at higher noise levels like 30 while preventing significant blurring of edges.
* The filter smooths regions with uniform intensity while keeping the essential structural features intact.

1. Quality Performance Analysis

5.1) Voxel Squared Error Difference

We compute the voxel squared error difference between the original brain image and the denoised image by the GPAD filter (**getVoxelSquaredErrorDifference**) for each level of noise (10,20 and 30). Then, we plot the voxel squared error difference for each level of noise and slice 102 and 119 (**plotVoxelSquaredErrorDifference**).

We show the error difference using a color map with a gradient color defined as red being the highest squared error and blue the lowest. It allows us to visually compare the performance of the GPAD filter under various noise levels (**Fig. 5**).

A blue squares with white text

Description automatically generated

**Fig. 5:** The first row is the voxel squared error difference for slice

102 and 119. Subsequent rows have similar content for noise level

20 and 30.

Overall, these plots are predominantly blue with some lighter dots, indicating that the GPAD filter maintains a generally low squared error difference per voxel, demonstrating its effective noise suppression, especially at lower noise levels. The color bar range increases significantly as noise levels increase, revealing more pronounced voxel error differences:

* For **slice 102**, the maximum voxel squared error difference starts at approximately **2000** for noise level 10 and rises to nearly **20,000** at noise level 30.
* For **slice 119**, the maximum error at noise level 10 is about **1800**, escalating to around **18,000** at noise level 20.

These observations indicate the challenge faced by the GPAD filter as noise levels rise, highlighting its limitations when handling high-noise images.

Despite these differences, the voxel squared error difference range being similar for both slices suggests that the GPAD filter handles various edge types consistently. This indicates that it preserves structural detail effectively.

To improve performance, further parameter tuning or the incorporation of additional filtering steps might be necessary.

5.2) Mean Square Error

We compute the Mean Square errors for the three noise levels and the five filters (**getRMSE**) and plot it (**plotRMSE**) (Fig.6).

This plot that shows:

* Overall, as the noise level increases, the MSE values for all filters increase, indicating that higher noise levels result in greater errors, regardless of the filter used.
* At the lowest noise level (10), the bilateral, Perona-malik and GPAD filters have the lowest MSE (**~0**) followed by the Gaussian and median filters.
* The **GPAD** filter MSE increases significantly with the level of noise; finishing with the worst MSE (**37**) among all the filters; indicating that it is not handling the noise efficiently with its current parameter configuration and may need more tuning (T,dt, σg, σs).
* By comparison, the **bilateral filte**r has a low MSE (**0**) at noise level 10 and its MSE increases the less among all the filters (**MSE:33 at noise level 30**); suggesting it is better at handling increased level of noise and the smoothed image quality is closest to the original image even at higher noise levels.
* The **Gaussian Filter** maintains a moderate MSE increase and appears to be competitive, especially at higher noise levels, being at the same MSE than the bilateral filter at noise level 30 (**MSE:33**).
* The **median filter** initially performs worse than the Gaussian filter (**MSE: 22 at noise level 10**) but still shows a less severe increase in MSE (**34**) at noise level 30 compared to the Perona-Malik and GPAD filters
* **The Perona-Malik filter** shows the lowest MSE at noise level 10 (**0**), demonstrating its effectiveness in edge preservation and noise reduction at lower noise levels. However, its MSE increases rapidly like the GPAD filter (**MSE:36 at noise level 30**). Again, this suggests that while the Perona-Malik filter is initially effective, it may not handle high noise levels as efficiently, when using the current parameter configuration (α, κ, T).

A graph with colored lines and text

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**Fig. 6:** MSE for Different Levels of Noise and

filters: Gaussian, Median, Bilateral, Perona-Malik

and GPAD Filter.

# Challenges

* The Geometry Preserving Anisotropic Diffusion filter is a complicated filter complex to implement. It has a larger number of critical sections quite intricated, and careful attention to detail is essential to ensure the accuracy and effectiveness of its implementation.
* It was slow to run and needed some code optimizations to increase its processing time and overall efficiency.

# Future Directions

* The different filter parameters (T,dt, σg , σs including the diffusion parameters: a1 and a2), could be tuned further using a more exhaustive grid search and for loss function the voxel squared error difference, or other loss functions related to image quality assessment (IQA) metrics (for ex., Peak Signal to Noise Ratio (PSNR), Mean Absolute Error (MAE), and Structural Similarity Index (SSIM)).
* **T Stopping Criterion**: The filter is iterative and runs for a fixed number of iterations (T). A more sophisticated stopping criterion that halts the process when a convergence or condition is met, such as when the rate of change in the image error becomes minimal.
* **Hybrid approach**: a first deep learning model extracts features of interests from properly annotated datasets by physicians or pathologists followed by a deep learning model having a second order optimizer based on a loss which could mimic the intensity gradient landscape.

Specifically:

1. **A Deep Learning Model for Feature Extraction**: A deep learning model, such as a convolutional neural network (CNN), is trained on annotated datasets curated by experts like physicians or pathologists. This model learns to identify and extract features of interest (e.g., edges, tissue boundaries, lesions) from medical images. By leveraging expert annotations, the model gains an understanding of key structures that should be preserved during the filtering process.
2. **A Gradient-Based Loss Function**: A secondary deep learning model is integrated with a second-order optimization approach, in which the loss function is designed to reflect the intensity gradient landscape. The optimizer utilizes second-order derivatives (e.g., Hessian-based approaches) to refine the filtering process, aligning it with the intensity gradient landscape learned from the feature extraction model.

This is the approach followed by Rodrigo Caye Daudt et al., who propose an iterative learning method to extract useful features from large datasets using a CNN to guide an anisotropic diffusion algorithm to perform edge preserving filtering [1].

**Reference**

[1] Rodrigo Caye Daudt, Bertrand Le Saux, Alexandre Boulch, and Yann Gousseau. 2021. Weakly supervised change detection using guided anisotropic diffusion. Mach. Learn. 112, 6 (Jun 2023), 2211–2237. https://doi.org/10.1007/s10994-021-06008-4